

Physics 640  
October 21, 2008

Project 4

**Week 7 & 8:**

-Introduction to Molecular Dynamics/Metropolis Algorithm/Monte Carlo

Molecular Dynamics:

Numerical algorithm to solve Newton's equations:

$$-\frac{d\Phi}{dt} = f = m\ddot{x} = m\frac{d^2x}{dt^2}$$

where  $\Phi$  is the interaction potential between molecules. Typical interaction potential between molecules are:

- Hard spheres
- Hooke's Law
- Lennard-Jones

The Lennard-Jones interaction between two molecules located at  $x_1$  and  $x_2$  is (no external forces are considered!):

$$\Phi(x_1, x_2) = \frac{1}{|x_1 - x_2|^{12}} - \frac{2}{|x_1 - x_2|^6}$$

This potential is repulsive at short distances and no interacting at large distances between molecules, being the point of minimum potential at mid range.

Assuming equal masses molecules, for a system of 4 molecules, we need to solve the following equations:

$$1) m \frac{d^2 x_1}{dt^2} = -\frac{d\Phi}{dx_1} = 12 \sum_{j=2}^4 \left[ \frac{1}{(x_1 - x_j)^{13}} - \frac{1}{(x_1 - x_j)^7} \right]$$
$$2) m \frac{d^2 x_2}{dt^2} = -\frac{d\Phi}{dx_2} = 12 \sum_{j=1,3,4} \left[ \frac{1}{(x_2 - x_j)^{13}} - \frac{1}{(x_2 - x_j)^7} \right]$$

3)...

4)...

-Use finite-difference to approximate the derivatives

-The differential equations of 2<sup>nd</sup> order require two initial conditions for each molecule: position and velocity

Example in this input file "md.in" for "molec\_dyn.f"

```
4 0.001 0.10 60.0
 0.50 0.00 0.00
-1.00 0.00 -0.00
-0.50 0.00 0.00
 1.00 0.00 -0.00
 0.00 -1.00 0.00
 0.00 0.00 1.00
 0.00 1.00 0.00
```

```

0.00 0.00 -1.00
* NATOM -Number of atoms (IN) is 4
* H - Time step. (IN) is 0.001
* HP - Time interval between printing. (IN) is 0.10
* TEND - Time at end of computation: TEND = H*NSTEP. (IN) is 60
* The next 8 lines specify the initial positions (cartesian
coordinates) and velocities of the atoms

```

Example output file "md.out"

```

4
600
0.000000 0 -4.078430E+00 2.000000E+00 -2.078430E+00
0.000000 1 5.000000E-01 0.000000E+00 0.000000E+00
0.000000 1 -1.000000E+00 0.000000E+00 0.000000E+00
0.000000 2 -5.000000E-01 0.000000E+00 0.000000E+00
0.000000 2 1.000000E+00 0.000000E+00 0.000000E+00
0.000000 3 0.000000E+00 -1.000000E+00 0.000000E+00
0.000000 3 0.000000E+00 0.000000E+00 1.000000E+00
0.000000 4 0.000000E+00 1.000000E+00 0.000000E+00
0.000000 4 0.000000E+00 0.000000E+00 -1.000000E+00
0.000000 0 -3.617130E+00 1.538704E+00 -2.078426E+00
0.100000 1 4.475015E-01 0.000000E+00 0.000000E+00
0.100000 1 5.895949E-01 0.000000E+00 0.000000E+00
0.100000 2 -4.475015E-01 0.000000E+00 0.000000E+00
0.100000 2 -5.895949E-01 0.000000E+00 0.000000E+00
0.100000 3 0.000000E+00 -9.753933E-01 9.917767E-02
0.100000 3 0.000000E+00 4.894474E-01 9.754606E-01
0.100000 4 0.000000E+00 9.753933E-01 -9.917767E-02
0.100000 4 0.000000E+00 -4.894474E-01 -9.754606E-01
.....

```

```

WRITE(3,99)INT(1000.*K*H),0,PE,KE,PE+KE
DO I = 1,NATOM
  WRITE(3,99)K*H,I,X(I),Y(I),Z(I)
  WRITE(3,99)K*H,I,U(I),V(I),W(I)
END DO

```

(where k is from the time looping)

\*NATOM is 4

\*NSTEP is 600

\*Then for each time iteration line "0" contains information on PE, KE, and PE+KE for all atoms

Outcomes for Project 4 part a), to be included in the report:

- 1) Animation of the position of a chosen number of molecules (4 or higher) over time given at least two different initial conditions. You should be able to confirm a result from your intuition in these animations based on the initial conditions. Explain in report.
- 2) Animate the motion of one of the molecules in phase space (x and  $v_x$ )