

Problem 11.13

Sketch the magnitude characteristic of the bode plot for the transfer function.

$$H(j\omega) = \frac{100(j\omega)}{(j\omega + 1)(j\omega + 10)(j\omega + 50)}$$

Suggested Solution

$$H(j\omega) = \frac{\frac{1}{s}(j\omega)}{(j\omega + 1)(\frac{j\omega}{10} + 1)(\frac{j\omega}{50} + 1)}$$

Problem 11.18

Sketch the magnitude characteristic of the bode plot for the transfer function.

$$H(j\omega) = \frac{100(j\omega)^2}{(j\omega + 1)(j\omega + 10)^2(j\omega + 50)}$$

Suggested Solution

$$H(j\omega) = \frac{100(j\omega)^2}{(j\omega+1)(j\omega+10)^2(j\omega+50)}$$

$$H(j\omega) = \frac{(1/50)(j\omega)^2}{(j\omega+1)(0.1j\omega+1)^2(0.02j\omega+1)}$$

poles : 1, 50 and 2 @ 10 r/s

zeros: 2 @ dc

also: $1/50 = -34$ dB

Problem 11.29

Find $H(j\omega)$ if its amplitude characteristic is shown in fig 29.

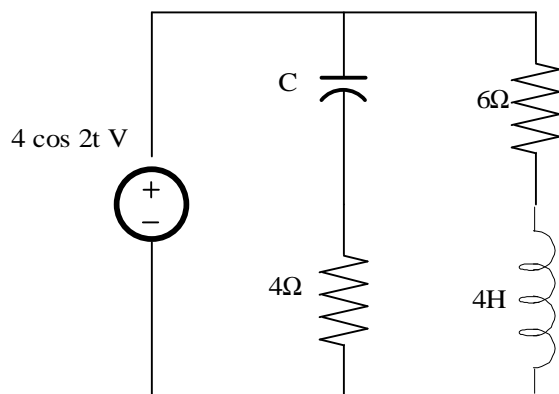
Suggested Solution

The initial slope of -20 dB/dec will cut the 0 dB line at $\omega=40$ r/s. Therefore the gain is 40. The zeros are at $\omega=50$ r/s and $\omega=1000$ r/s. The poles are at $\omega=0$ and there is a double pole at $\omega=400$.

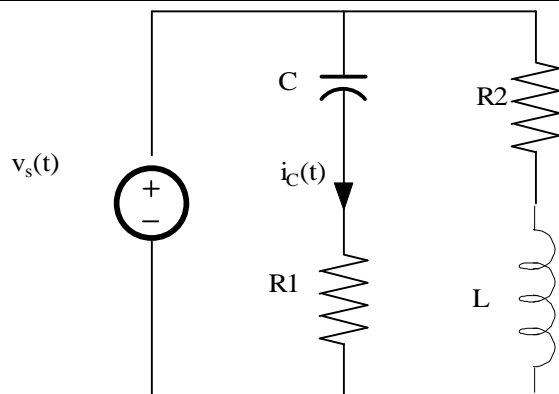
$$H(j\omega) = \frac{40\left(\frac{j\omega}{50} + 1\right)\left(\frac{j\omega}{1000} + 1\right)}{j\omega\left(\frac{j\omega}{400} + 1\right)^2}$$

Problem 11.50

Determine the value of C in the network shown in fig 11.50 in order for the circuit to be in resonance.



Suggested Solution



AT RESONANCE $V_s(t)$ AND $I_s(t)$ ARE IN PHASE.
SO, THE IMPEDANCE SEEN BY THE SOURCE, Z_s , IS PURELY RESISTIVE.

$$Z_s = \left(R_1 + \frac{1}{j\omega C} \right) \parallel \left(R_2 + \frac{1}{j\omega L} \right) = R_{EQ} + j0$$

$$Z_s = \left(4 + \frac{1}{j2C} \right) \parallel (6 + j8)$$

$$Z_s = \frac{24 + \frac{4}{C} + j(32 - \frac{3}{C})}{10 + j(8 - \frac{1}{2C})} = \frac{N(j\omega)}{D(j\omega)} = R_{eq}$$

IF Z_s IS RESISTIVE, THEN THE PHASE ANGLES OF $N(j\omega)$ AND $D(j\omega)$ MUST BE EQUAL.

$$\frac{32 - 3/C}{24 + 4/C} \Rightarrow 64C^2 - 25C + 1 = 0 \Rightarrow C = 45.2\text{mF}, 345.4\text{mF}$$